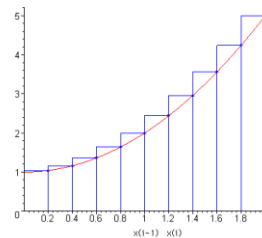
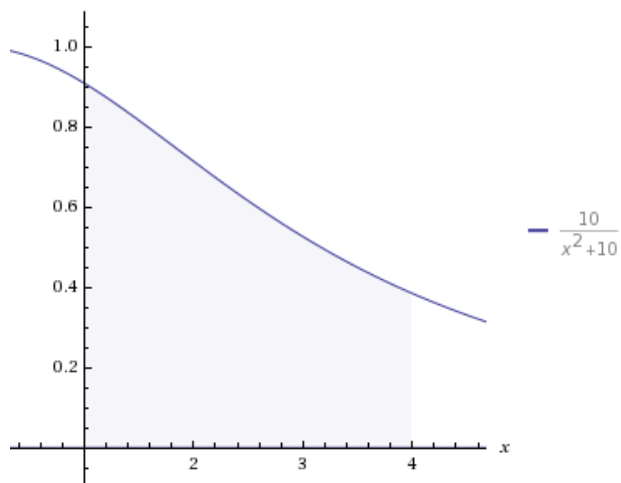




## Riemann Sum = Super Fun!



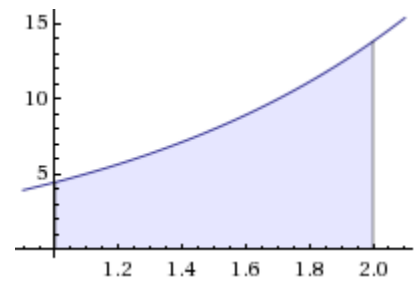
1. Find the approximate area under the function  $y = \frac{10}{10+x^2}$ , from  $x = 1$  to  $x = 4$   
(Use 6 rectangles;  $n=6$ )  
(**answer: around 1.75ish**)



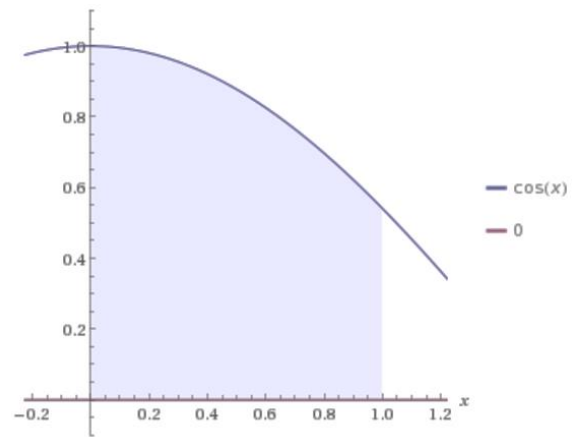
2. Use a Riemann sum to estimate the area between  $f(x) = 0.25x^3$  and the  $x$ -axis along the interval  $[4,7]$  Use four rectangles.  
**Before you start:** use a graphing utility or the internet to sketch the area you are trying to find...no sketch...no marks  
(**answer: 161.38 ish**)

3. Compute the approx. area between  $f(x) = \sin x$  and the x-axis from 0 to  $\pi$ .  
Use  $n=5$ . **Draw a sketch of this area.**  
*(answer: 1.93ish)*

4. Find the approx area below  $y = 2e^x - 1$  from 1 to 2. Use  $n = 4$ .  
*(answer: 9.56)*



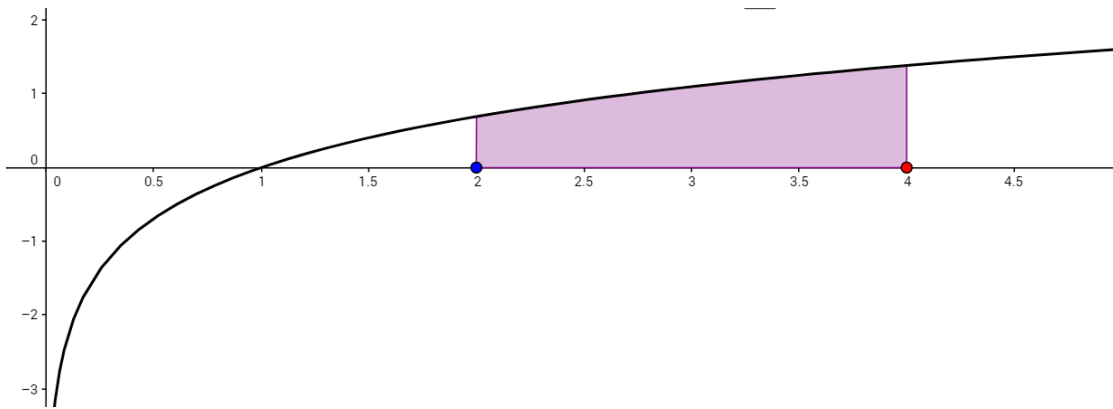
5. Find the area under the function  $\cos x$  from (0 to 1). Use 4 rectangles.  
(Answer: 0.78)



6. Find the area under  $\ln x$  from 2 to 4 using the following methods:

- a) First just look at the graph and estimate the area
- b) Use a Riemann sum with 3 rectangles
- c) Use a Riemann sum with 6 rectangles
- d) Use a Riemann sum with 9 rectangles

**Show all your work.**



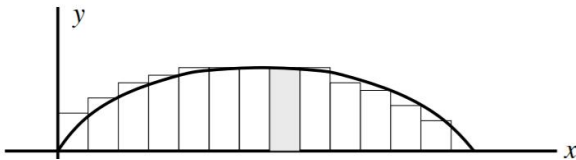
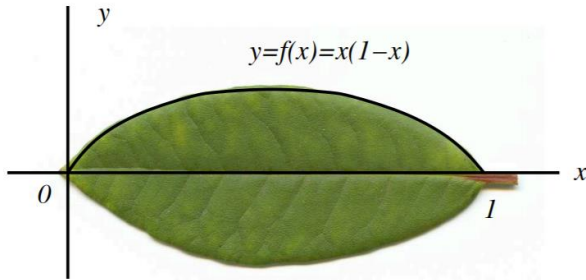
**Answer is approx. 2.16 unit<sup>2</sup>**

7. Find the area under  $f(x) = 2/(1+x)$  from 1 to 2 with  $n=6$   
*Draw a sketch.*

*Answer: 0.78*

**Bonus:** (1 mark each)

1. Find the area of the leaf shown below given that the top edge of the leaf adheres to the function  $f(x)$  shown in the diagram (**use 14 rectangles**). Answer: approx,  $1/3$  units<sup>2</sup> (note: you will have to double the area you initially find (leaf is symmetrical over x-axis)).



2. Determine the area that is enclosed between the functions  $f(x) = e^x$  and  $f(x) = x$

Between 0 and 1 use  $n = 5$

